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Art of Thinking

Pigeonhole Principle

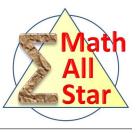


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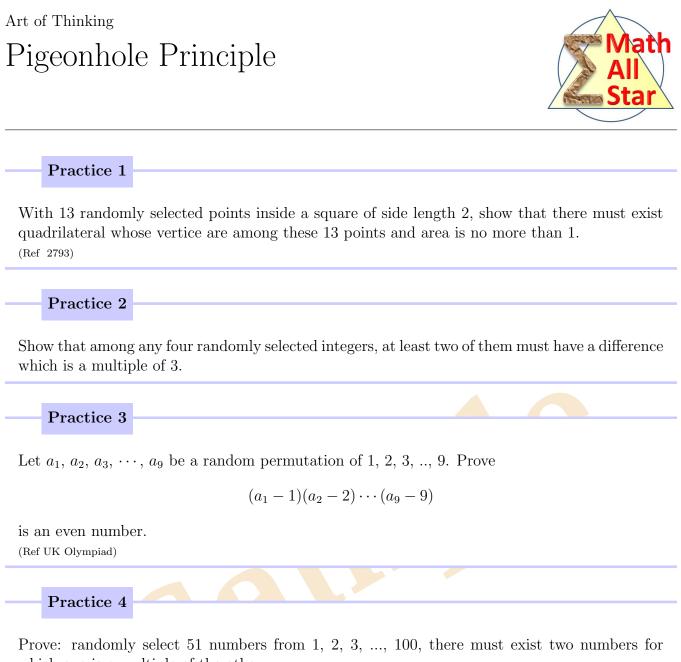
Instructions

- Write down and submit intermediate steps along with your final answer.
- If the final result is too complex to compute, give the expression. e.g. C_{100}^{50} is acceptable.
- Problems are not necessarily ordered based on their difficulty levels.
- Always ask yourself what makes this problem a good one to practise?
- Complete the My Record section below before submission.

My Comments and Notes



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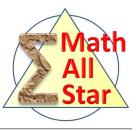
Prove: randomly select 51 numbers from 1, 2, 3, ..., 100, there must exist two numbers for which one is a multiple of the other. (Ref 1119)



Show that it is possible to find an integer whose digits are all 8 and it is a multiple of 2016. (Ref 2792)

Practice 6

Prove: any convex pentagon must have three vertex A, B, and C, such that $\angle ABC \leq 36^{\circ}$. (Ref 2105) Art of Thinking Pigeonhole Principle



Battle Field

Here are some related problems selected from recent comptitions:

Problem 1: 2012 MathCounts State Target #5

Problem 2: 2002 AMC10P #15